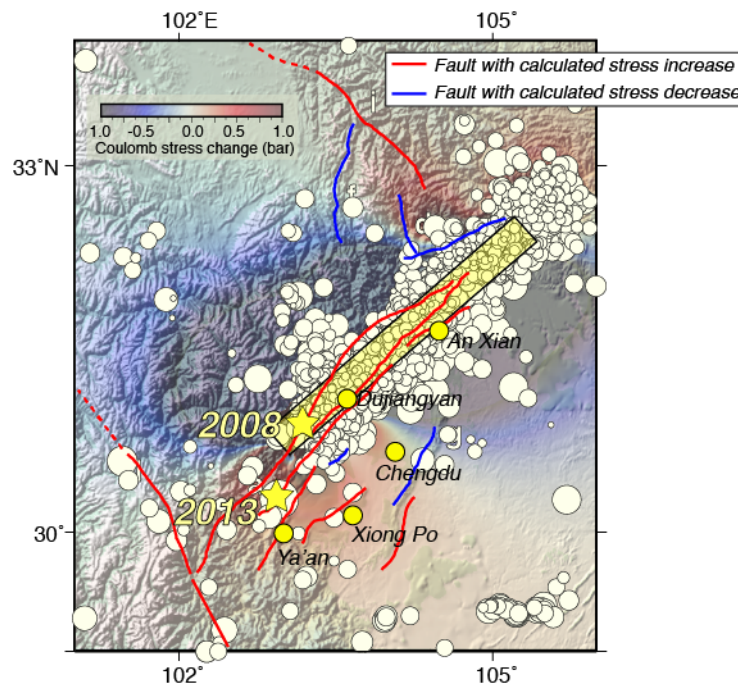


# ***Stress, Distance, Magnitude, and Clustering Influences on the Success or Failure of an Aftershock Forecast: the 2013 M=6.6 Lushan Earthquake and Other Examples***

by Tom Parsons<sup>1</sup> and Margarita Segou<sup>2</sup>

## **INTRODUCTION**

Immediately after the 12 May 2008  $M=7.9$  Wenchuan earthquake, we began calculating the static stress change on major faults surrounding the rupture zone (Parsons *et al.*, 2008), and Toda *et al.*, (2008) mapped out regional Coulomb stress changes (Fig. 1). The purpose was two-



**Figure 1.** Earthquake activity ( $M \geq 2$ ) following the 12 May, 2008  $M=7.9$  Wenchuan mainshock in Sichuan Province, China. Epicenters are superposed on static stress change calculations made shortly after the mainshock in 2008 on mapped faults (red and blue lines) and optimally oriented faults (Parsons *et al.*, 2008). It is evident that many aftershocks occurred in regions/faults with calculated stress decreases, which led Parsons *et al.* (2012) to conclude that the forecast was a failure.

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fold: (1) to identify the most likely locations (stress increases) of dangerous aftershocks, and (2) to conduct a prospective test of stress mapping as a rapid-response forecast tool. The occurrence of the 20 April 2013  $M=6.6$  Lushan earthquake in the Longmen fault zone near Ya'an was consistent with the prospective static stress forecast; for example press coverage in 2008 ([Kuang, 2008](#)) stated:

*“According to their results, published in Nature on 6 July, Ya'an Thrust, Xiong Po Thrust, and Xianshuihe Fault, all near Longmen Fault where the earthquake occurred, show a notable increase in static stress changes, and therefore face a high risk of aftershocks.*

*‘The 12 May earthquake ... caused grievous losses, yet its legacy includes possible large aftershocks in the near future because it increased failure stress on important faults within and around the Sichuan basin,’ write the authors.*”

However, a formal evaluation of the post Wenchuan forecast performance by [Parsons et al. \(2012\)](#) was not favorable, as:

*“...we show two fully prospective static stress forecasts that have failed to reproduce spatial patterns of microseismicity ... over a span of 1 to 4 years we find that forecast spatial distributions of earthquakes are violated, with clear rate increases in stable stress-shadowed zones at Kashmir, and at Wenchuan.”*

Indeed, a visual examination of Figure 1 shows many examples of aftershocks occurring at high rates in stress shadow (calculated decrease) areas where the expectation would have been a seismicity rate decrease.

The 2013 Lushan earthquake caused 203 deaths, injured at least 11,492, and affected more than 1.5 million others ([UNICEF China, 2013](#)). We consider the Lushan event as an aftershock of the 2008 Wenchuan mainshock per [Scholz \(2002\)](#), who defines them as

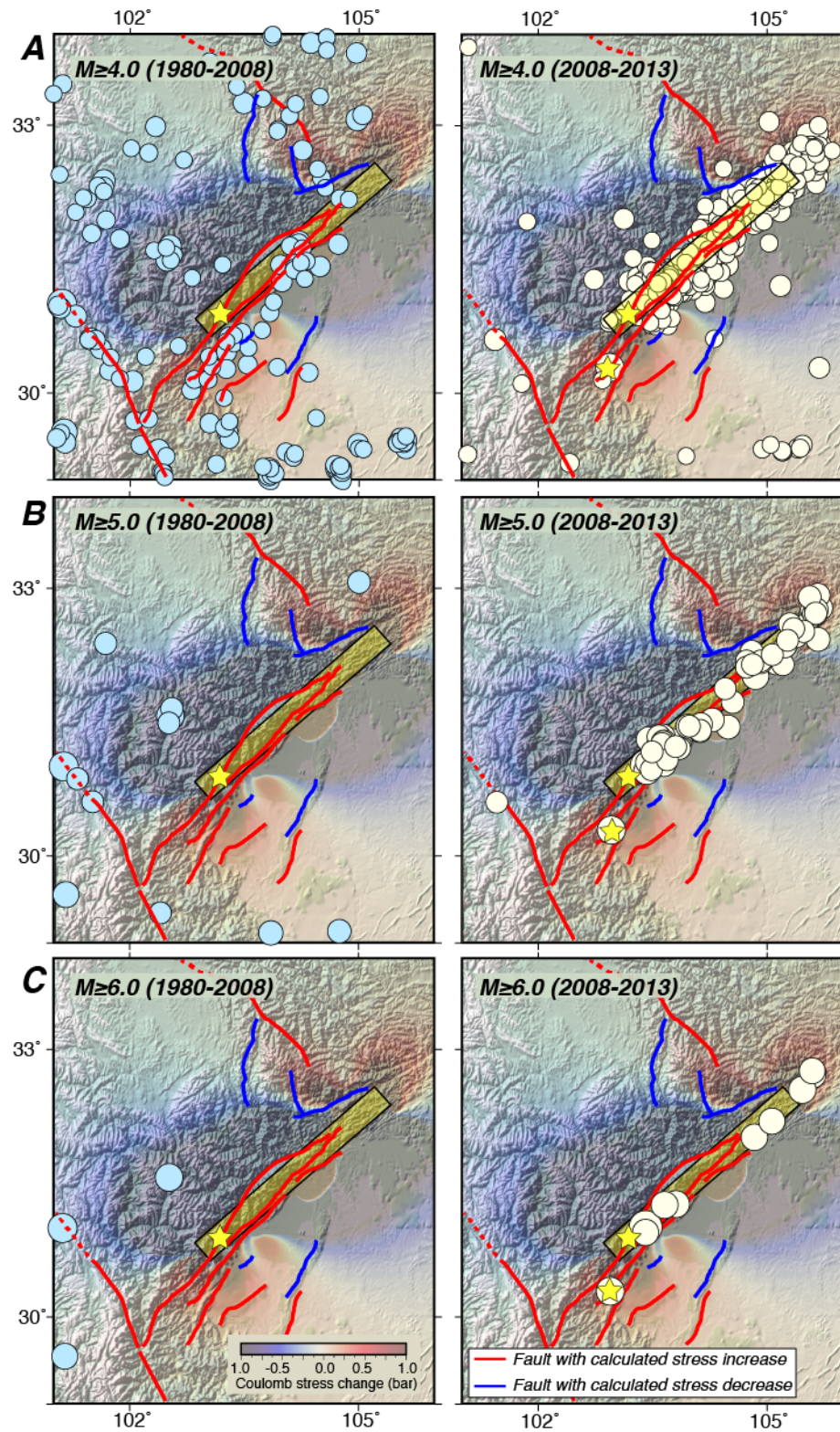
*“Aftershocks typically begin immediately following the mainshock over the entire rupture area and its surroundings, although they are commonly concentrated in locations where one where one might expect large stress concentrations to have been produced by the mainshock rupture.”*

Additionally, [Parsons \(2002\)](#) cataloged thousands of  $M > 5$  stress-triggered earthquakes that occurred up to 240 km away from mainshock ruptures, and that that behaved like aftershocks with Omori-law temporal decays that persisted for 7-11 years after mainshocks in a global study.

Where and when the 2013  $M=6.6$  Lushan earthquake happened raises two key questions: are static stress change calculations more applicable to larger aftershocks? Are empirical forecasts (those based on observed activity levels and known temporal and spatial aftershock behaviors) always better than stress-based methods? A single case such as the Wenchuan-Lushan pairing is not necessarily representative, so we look at additional large continental earthquakes and their aftershock relationships.

## **AFTERSHOCK DISTRIBUTION OF THE 2008 $M=7.9$ WENCHUAN EARTHQUAKE**

As is typical following a large earthquake, the spatial distribution of seismicity was strongly altered by the 2008  $M=7.9$  Wenchuan event (Fig. 2). The highest magnitude aftershocks are located closest to the mainshock rupture, and are consistent with calculated Coulomb stress change calculations. There are many aftershocks of  $M \geq 4.0$  that occurred in calculated stress shadow regions (Fig. 2a), but when the threshold is increased to  $M \geq 5.0$ , and especially  $M \geq 6.0$ , all aftershocks are located within a few km of the mainshock rupture (Fig. 2). That the largest aftershocks tend to be nearest to mainshocks has been noted previously at Wenchuan (e.g., [Lü \*et al.\*, 2008](#); [Shi \*et al.\*, 2009](#)) and other places (e.g., [Nanjo and Nagahama, 2000](#); [Chen and Wang,](#)



**Figure 2.** Earthquake activity for different magnitude thresholds shown before and after the 12 May, 2008  $M=7.9$  Wenchuan mainshock. Blue dots represent 1980-2008 events,

whereas yellow are 2008-present. The same stress change patterns are shown as in Figure 1. As lower magnitude events are excluded, the fit to stress change patterns improves. The highest magnitude events are only found near the mainshock rupture (approximated by the yellow rectangle).

2012; Tahir *et al.*, 2012), though Eneva and Pavlis (1991) and Doser (1989) found null or opposite cases. One argument for larger aftershocks being located on or near the mainshock rupture might be that is where the longest faults are likely to be. However, in the case of the Wenchuan setting, there are many distant faults with calculated stress increases capable of generating  $M \geq 6.0$  earthquakes as can be seen from the pre-2008 catalogs shown in Figure 2.

From an admittedly small sampling, it might be hypothesized that the static stress based forecast in the Sichuan Basin is most effective, or only effective, for higher magnitude aftershocks. Reasons for this might include the following: (1) it may be that high static stresses ( $\geq 1$  bar) tend to be required to trigger large aftershocks, (2) in the Wenchuan case, almost all of the faults nearby the mainshock rupture were calculated to have increased failure stress (Fig. 2), and/or (3) The unknown contributions of dynamic triggering by seismic waves (e.g., Felzer and Brodsky, 2006; Richards-Dinger *et al.*, 2010) may overprint the static stress change effect, and may only apply to lower magnitude triggered events (Parsons and Velasco, 2011).

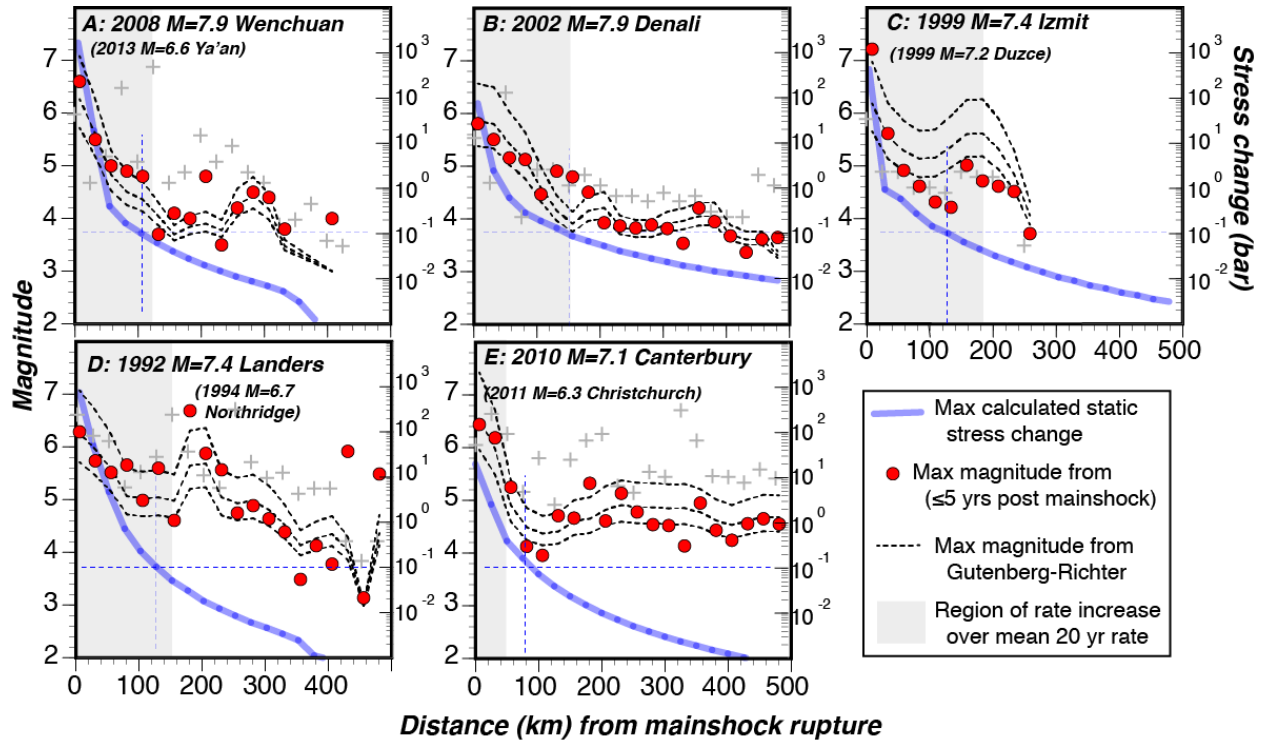
From Figure 2 it is also evident that most high magnitude aftershocks happened in areas with the highest overall aftershock activity levels (clustering). Therefore the maximum aftershock magnitude may have no direct relationship to the stress change amplitude, but instead may only be a consequence of increased activity. Such clustering behavior forms the basis of highly successful empirical aftershock forecasting methods such as Epidemic Type Aftershock Sequence (ETAS) modeling (Ogata, 1988; 1998).

It would obviously be difficult to settle these often debated points here, but some insight into the generality of observations at Wenchuan can be gained by looking at aftershocks of comparable continental earthquakes. The idea is to see if there is a similar dependence of highest magnitude aftershocks with distance to the mainshock rupture surface, and to test correlations between highest calculated static stress change, clustering, and aftershock magnitude.

### **$M_{max-aftershock}$ VS. DISTANCE, MAXIMUM STRESS CHANGE, AND CLUSTERING FOR SELECTED MAINSHOCKS**

We examine aftershock and static stress change characteristics for four additional  $M=7.1$  to  $M=7.9$  continental earthquakes: the 1992  $M=7.4$  Landers, 1999  $M=7.4$  Izmit, 2002  $M=7.9$  Denali, and 2010  $M=7.1$  Canterbury shocks (Fig. 3). These events were selected because they are in similar settings to the Wenchuan mainshock, and have comparable magnitudes and network catalogs. No mainshocks were considered that aren't presented here.

We used the following procedure to produce the plots in Figure 3: (1) we simplified the ruptures to a single plane and calculated distances from those planes to every aftershock from a 5 year period (except the Canterbury event, which has a  $\sim 3$  year duration), (2) we find the maximum aftershock magnitude ( $M_{max-aftershock}$ ) in 20 km distance bins between 0 to 500 km, (3) we calculated static Coulomb stress change from each rupture resolved on optimally oriented planes using a friction coefficient of  $\mu=0.4$ , and tectonic stress orientations taken from the mainshocks, (4) we found the maximum Coulomb stress increase in the same 20-km distance bins as  $M_{max-aftershock}$  determinations, (5) we calculated the expected maximum aftershock



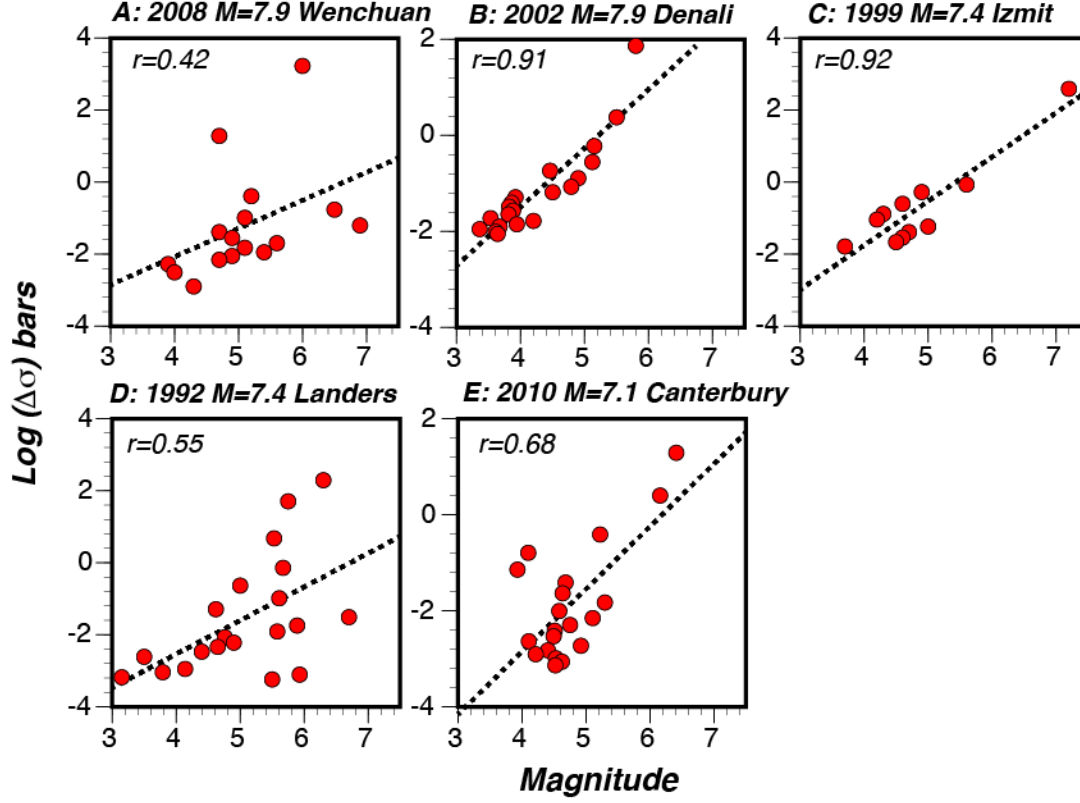
**Figure 3.** Maximum observed earthquake magnitude (red dots) vs. distance from rupture surface for a group of  $M \geq 7$  continental earthquakes. Dashed black lines show calculated expected maximum magnitude vs. distance as extrapolated from Gutenberg-Richter relations with  $b$ -values ranging from 0.8 to 1.2. Heavy blue lines show calculated maximum Coulomb stress change vs. distance. Gray shaded regions show approximate extents of calculated earthquake rate increase above 20-year means. The horizontal dashed blue line shows the +0.1 bar stress change threshold, and the vertical dashed blue line marks the distance from the mainshock planes where that occurs, which tends to be located fairly close to the earthquake rate-increase threshold. Gray “+” symbols show maximum observed magnitudes vs. distance that occurred in the 20 year periods before mainshocks.

magnitude by linear extrapolation of Gutenberg-Richter relations ( $\log(N)=a-bM$ , with  $b$ -values from 0.8 to 1.2, and  $a$ -values taken from observed rates) of aftershocks in the 20-km distance bins, (6) we used the  $\sim 20$ -yr pre-mainshock catalogs to find the maximum observed magnitudes in the same distance bins to gain insight into what magnitudes might be possible vs. distance, and (7) the distance range from mainshock ruptures where the mean aftershock seismicity rate (events per year) is higher than the pre-mainshock mean is calculated as a guideline.

The purpose for making the above-described calculations is to compare the generalized distance reach of the static stress increase and activity levels (clustering) with  $M_{max-aftershock}$  values for a number of different earthquakes to establish whether there is a consistent trend that is similar to the observations plotted in Figure 2. The Coulomb stress calculations are subject to parameter uncertainty that affects the specific mapped patterns of stress change. In this instance the primary feature of interest is an expression and comparison of the falloff of maximum stress change vs. distance in a general way. Therefore the details of the calculations are less important than uniformity of approach for each event.

From the resulting plots it is clear that the maximum aftershock magnitudes tend to occur closest to the mainshock ruptures and decay with distance (Fig. 3). For most of the mainshocks, the slope of  $M_{max-aftershock}$  falloff is steepest in the first 100 km away from mainshock ruptures. This change in slope is also associated roughly with the range of post-mainshock seismicity rate increase, and the 0.1 bar maximum stress change increase that has been suggested as a minimum necessary to cause triggering (e.g., [Reasenbergs and Simpson, 1992](#); [Hardebeck et al., 1998](#); [Harris, 1998](#)). This can be interpreted as a static stress change process operating across an approximate 80 to 200 km distance from mainshock ruptures with highest magnitude aftershocks corresponding to highest stress changes.

The apparent correlations between calculated Coulomb stress magnitude and  $M_{max-aftershock}$  in Fig. 3 can be quantified if the log maximum stress increase values vs. distance from the mainshock rupture plane are compared with the maximum magnitude aftershocks vs. distance. The distance binning is retained because it provides a means of isolating the maximum magnitude events. There is a significant empirical correlation between log stress change and  $M_{max-aftershock}$  for the investigated mainshocks (Fig. 4), with correlation coefficient ( $r$ ) values

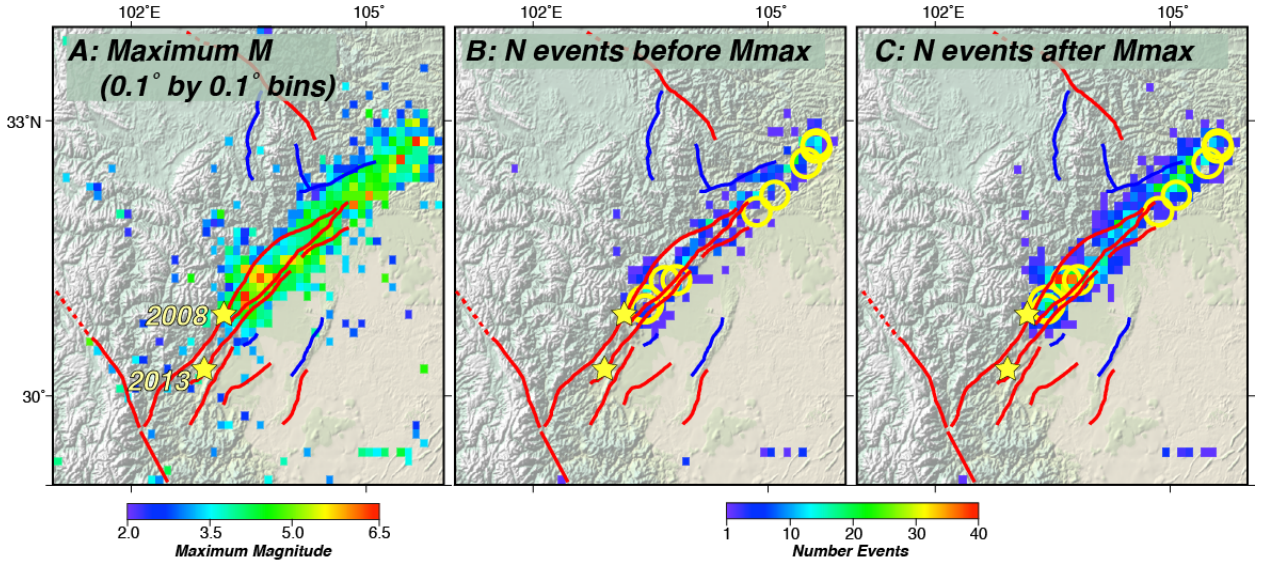


**Figure 4.** Plots show correlations between log stress change and maximum post-mainshock magnitudes observed in the same distance ranges as plotted in Figure 3. The -1 value on the vertical axis thus corresponds to the 0.1 bar stress change threshold. There is a significant relationship between the magnitude of stress change and earthquake magnitude. The correlation coefficients ( $r$ ) are given for each mainshock.

ranging from 0.42 to 0.92. While there is a defensible general correlation amongst distance, magnitude of stress change, and triggered earthquake magnitude, the observations are noisy enough that applying a higher stress change threshold than the traditional +0.1 bar value (e.g., Reasenberg and Simpson, 1992; Hardebeck *et al.*, 1998; Harris, 1998) would miss many  $M > 5$  aftershocks (Fig. 4). Empirically however, odds are that most high-magnitude triggered events will be found where stress changes are largest. However, it is also apparent that most triggered events of all magnitudes can be found where stress changes are largest (Fig. 3), and both quantities diminish with distance.

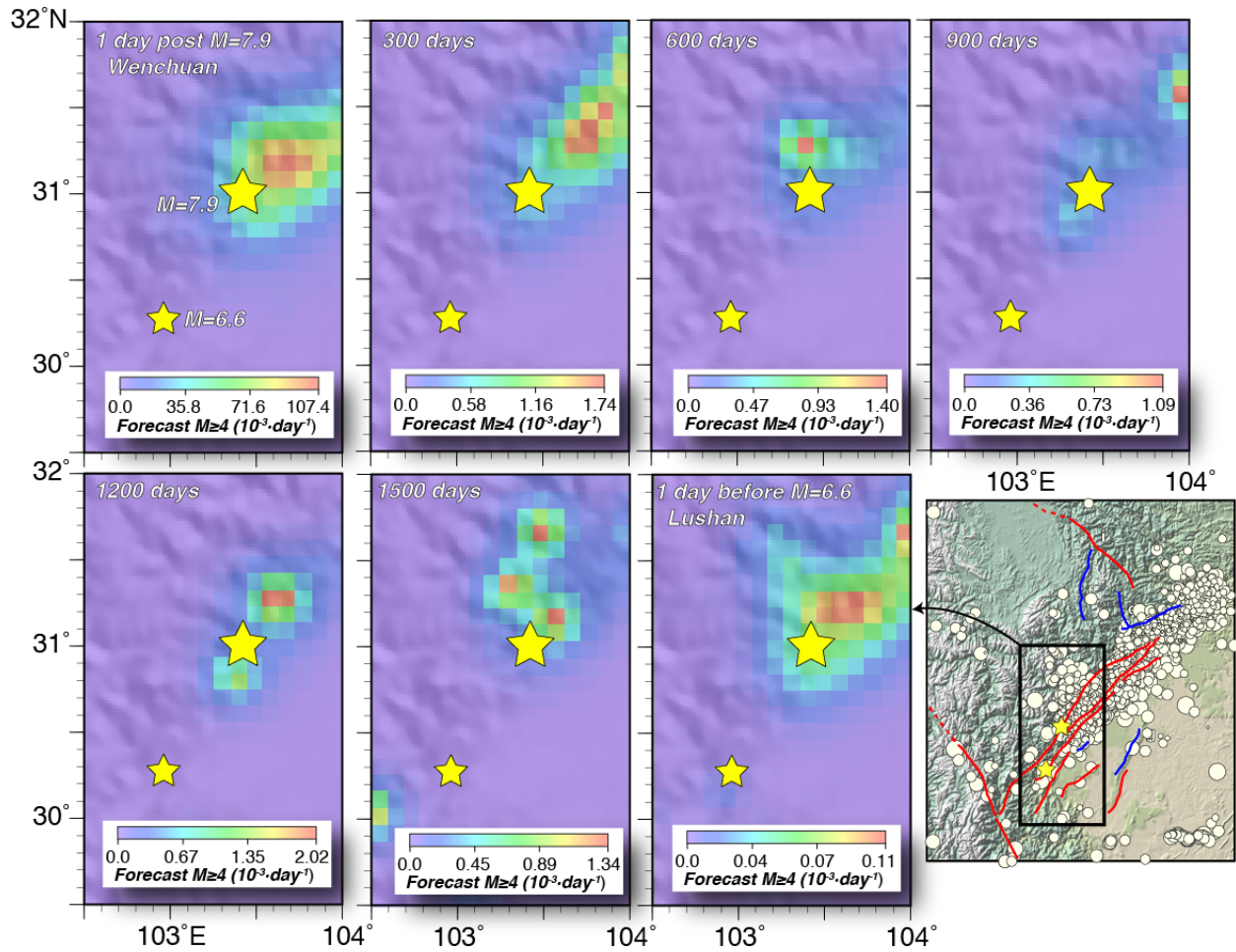
Observed  $M_{max\text{-aftershock}}$  values tend to fall within, or close to expected ranges calculated from extrapolations of the magnitude frequency distributions of smaller aftershocks (Fig. 3). This raises the question whether the true correlation is between stress change and  $M_{max\text{-aftershock}}$ , or instead with the aftershock activity level ( $a$ -value); if a Gutenberg-Richter relation applies, then the maximum expected magnitude is a direct function of the  $a$ -value. In other words, the actual correlation might be between stress change and aftershock clustering, with higher magnitude events being a byproduct.

To examine the spatial correspondence between activity levels and  $M_{max\text{-aftershock}}$  values more closely, we divided the Wenchuan region into  $0.1^\circ$  latitude by  $0.1^\circ$  longitude spatial bins (e.g., Lee *et al.*, 2011) and determined the maximum observed aftershock magnitudes in each bin. We then found the number of events that preceded the maximum magnitude aftershocks (Fig. 5). All but one of the  $M \geq 6$  aftershocks (which happens to be the 2013  $M=6.6$  Lushan event) occurred in areas of elevated prior activity (Fig. 5b). These results typify what is found from empirical forecast methods like ETAS (e.g., Ogata, 1988; 1998; Smyth *et al.*, 2010). In fact, using initial post-mainshock activity levels in time-space ETAS models usually outperforms stress based forecasting in formal evaluations (e.g., Woessner *et al.*, 2011; Segou *et al.*, 2013). However, for the Lushan case, the  $M=6.6$  shock was the first  $M > 2$  event to occur in the immediate vicinity (Fig. 5b), and it would thus have been difficult to anticipate from seismicity rate changes in an empirical forecast, as has been shown in Wenchuan and other regions (Fig. 6) (e.g., Shi *et al.*, 2009; Console *et al.*, 2010; Smyth *et al.*, 2010; Werner *et al.*, 2011; Hardebeck, 2013; Segou *et al.*, 2013).



**Figure 5.** Maps showing: (a) maximum aftershock magnitudes in  $0.1^\circ$  by  $0.1^\circ$  spatial bins during the 5 years following the 2008  $M=7.9$  Wenchuan mainshock, (b) the number of aftershocks preceding the  $M_{max\text{-aftershock}}$  in each bin, and (c) the number of events following the  $M_{max\text{-aftershock}}$ . Yellow circles show locations of  $M \geq 6.0$  aftershocks. Note the lack of prior activity near the 2013  $M=6.6$  Lushan earthquake.

We show sample space-time ETAS (Ogata, 1998)  $M \geq 4$  aftershock forecasts from different periods within the interval between the 2008  $M=7.9$  Wenchuan and 2013  $M=6.6$  Lushan earthquakes to illustrate the difficulty in anticipating the Lushan earthquake from an empirical basis (Fig. 6). We solved for parameters with a maximum likelihood method (Table 1), and made 30 day forecast calculations at 30-day intervals throughout the period between the two earthquakes. As expected from Fig. 5, there was no indication of enhanced likelihood of future  $M \geq 4$  events at the Lushan site during any interval (Fig. 6). Thus while empirical methods were very effective in identifying the spatial and temporal distribution of other  $M \geq 6$  events, they were limited in the Lushan case by the dearth of prior activity.



**Figure 6.** Example maps showing 30-day  $M \geq 4$  forecast rates in  $0.1^\circ$  by  $0.1^\circ$  spatial bins for different times during the 5 years following the 2008  $M=7.9$  Wenchuan mainshock using the time-space ETAS method (Ogata, 1998). Warm colors indicate the highest expected  $M \geq 4$  rates; scales are different for each period because of the regional Omori-law decay. At no time after the 2008 mainshock does the location of the 2013  $M=6.6$  Lushan earthquake show a high expected  $M \geq 4$  rate because of the lack of precursory activity as noted in Fig. 5. The inset map shows the location of the forecast area.

$K$	$c$	$\alpha$	$p$	$d$	$q$	$b$	branching ratio
events/day/degree <sup>2</sup>	day	magnitude <sup>-1</sup>		degree <sup>2</sup>			
0.13	0.01	0.8	1.2	0.0071	1.96	1.0	0.57

**Table 1.** Maximum likelihood estimates of space-time ETAS parameters used to forecast  $M \geq 4$  aftershocks in the Wenchuan region. Parameters  $K$ ,  $c$ , and  $p$  are Omori-law values governing the decay rate of aftershocks,  $\alpha$  estimates the magnitude efficiency of an earthquake in generating its offspring,  $d$  and  $q$  are spatial fitting parameters. The parameter  $b$  is the Gutenberg-Richter magnitude-frequency slope, and the branching

ratio is the estimated number of triggered events per mainshock. See [Ogata \(1998\)](#) for a full discussion.

## DISCUSSION

Does magnitude matter when evaluating a stress-based forecast? Are empirical forecasts always better? Static stress based methods appear effective for higher magnitude ( $M \geq 6$ ) aftershocks in the Wenchuan region, most notably the interaction between the 2008  $M=7.9$  mainshock and the 2013  $M=6.6$  Lushan event. Similarly, the 2010  $M=7.1$  Canterbury and 2011  $M=6.3$  Christchurch pairing in New Zealand ([Stramondo et al., 2011](#)), and the 1999  $M=7.4$  Izmit and  $M=7.2$  Duzce shocks in Turkey ([Hubert-Ferrari et al., 2000](#); [Parsons et al., 2000](#)) are consistent with static stress change models. A potential exception is the 1992  $M=7.4$  Landers and 1999  $M=7.1$  Hector Mine earthquake pair in California, the hypocenters of which lie about 60 km apart. Parsons and Dreger ([2000](#)) suggested that the slip distribution of the Hector Mine event was influenced by stress change from the Landers mainshock, though Harris and Simpson ([2002](#)) found that most stress change models did not put the Hector Mine hypocenter in a stress increased zone. Globally, about 80% of  $M \geq 6.0$  aftershocks were found consistent with static stress change calculations using a 20-year centroid moment tensor catalog vs. 61% for  $M \geq 5.0$  shocks ([Parsons et al., 2012](#)).

By contrast, it has been more difficult to correlate static stress change calculations with the full magnitude spectrum (e.g., [Felzer and Brodsky, 2005](#); [Mallman and Zoback, 2007](#); [Hainzl et al., 2009](#)) (Fig. 1). This correlation is very likely complicated by multiple triggering mechanisms in the near field that include the static stress changes discussed here, as well as dynamic triggering by body waves (e.g., [Gomberg et al., 1997](#); [Kilb et al., 2000](#); [Felzer and Brodsky, 2006](#)), pore fluid flow (e.g., [Nur and Booker, 1972](#)), and viscoelastic stress transfer (e.g., [Melosh, 1976](#); [Pollitz and Sacks, 2002](#)).

Since the largest aftershocks are clearly the important ones to forecast correctly, the exercises in this paper point to three (likely not independent) considerations: (1) the most probable places that high magnitude aftershocks will occur are where there is the highest overall aftershock activity, (2) high magnitude aftershocks are most likely to happen where stress change calculations are greatest, and (3) high magnitude aftershocks are most likely to happen on well developed fault zones. All three of these points are fairly obvious, but the 2008  $M=7.9$  Wenchuan and 2013  $M=6.6$  Lushan pair highlights the devastating importance of exceptions. For example, if the Lushan earthquake is taken to have been correctly forecasted (Figs. 1, 2), then its location was predicted from geology and stress change calculations only. If forecasting were limited to considering post-2008 clustering, then the Lushan earthquake location would not have been anticipated (Figs. 5, 6). Our conclusion is that stress-based and empirical forecasts have limitations such that both need to be considered.

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